

Kinetics of Hydrolysis of Aziridines in Moderately Concentrated Mineral Acids. Relationship of ϕ Parameters to Reaction Mechanism¹

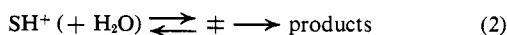
J. F. Bunnett,* Ray L. McDonald,² and Fredric P. Olsen³

Contribution from the Metcalf Chemical Laboratory, Brown University, Providence, Rhode Island, and the Thimann Laboratories, University of California, Santa Cruz, California 95064. Received September 4, 1973

Abstract: Rates of hydrolytic ring opening of aziridinium ion (**1a**) and 2-methylaziridinium ion (**1b**) diminish with increasing acid concentration in 1–6 *M* HClO₄. From **1b**, the fraction of 2-amino-1-propanol (**2b**) product decreases from about 65% in 1 *M* to 48% in 6 *M* HClO₄. 2,2-Dimethylaziridinium ion (**1d**) hydrolyzes faster than **1a** or **1b**. Rates of hydrolysis of **1d** are nearly constant in 1–4 *M* HClO₄ and 1–5 *M* H₂SO₄, but increase with further augmentation of acid concentration. The fraction of 2-amino-2-methyl-1-propanol (**2d**) product decreases from about 12% in 1 *M* acid to amounts too small to determine above 4 *M* HClO₄ or H₂SO₄. Plots of $\log k_{\psi}$ vs. ($H_0 + \log [H^+]$) are reasonably linear, except for hydrolysis of **1d** to 1-amino-2-methyl-2-propanol (**3d**) in HClO₄. The slopes (ϕ parameters) appear to be about -0.05 for reactions by the S_N1 mechanism and about $+0.35$ for S_N2 reactions, but special activity coefficient effects appear to intervene for **1d** hydrolysis in HClO₄.

The rates of acid-catalyzed reactions generally increase with the acid concentration, but the steepness of increase in moderately concentrated mineral acids (usually 1–10 *M* HCl, HClO₄, or H₂SO₄) is sharply dependent on the identity of the substrate. Also, as was first evident to Hammett in the 1930's,⁴ there is some relationship between the steepness of increase and the mechanism of the reaction which occurs.

For the familiar case of a weakly basic substrate (S), it is profitable to consider an acid-catalyzed reaction to comprise two idealized steps. Step 1 is equilibrium



protonation of the substrate. In step 2, the protonated substrate (SH⁺) reacts, sometimes with water, to form ultimate products, *via* a transition state (\ddagger).

The essential features of the problem are revealed by formulation of rate equations. Let us consider the rate of destruction of total substrate, $[S]_{st} = [S] + [SH^+]$. Phenomenologically

$$-d[S]_{st}/dt = k_{\psi}[S]_{st} \quad (3)$$

where k_{ψ} is the pseudo-first-order rate constant. Conceptually, with attention first to reaction step 2

$$-d[S]_{st}/dt = k_r^0[SH^+]\gamma_{SH^+}/\gamma_{\ddagger} \quad (4)$$

where k_r^0 is the rate constant for step 2 at infinite dilution in water and γ_{SH^+} and γ_{\ddagger} are activity coefficients. Utilizing the equilibrium constant expression for step 1, and substituting for $[SH^+]$ in eq 4, we obtain

$$-d[S]_{st}/dt = (k_r^0[S][H^+]/K_{SH^+}) \times (\gamma_S\gamma_H/\gamma_{SH^+})(\gamma_{SH^+}/\gamma_{\ddagger}) \quad (5)$$

(1) Investigation supported in part by the National Science Foundation and by the Army Research Office (Durham).

(2) Visitor at U. C. Santa Cruz, Jan–June, 1973, on sabbatical leave from the University of Hawaii.

(3) This paper is based in part on the Ph.D. Thesis of F. P. Olsen, Brown University, 1964.

(4) (a) L. Zucker and L. P. Hammett, *J. Amer. Chem. Soc.*, **61**, 2791 (1939); (b) L. P. Hammett, "Physical Organic Chemistry," McGraw-Hill, New York, N. Y., 1940, pp 267–277.

where K_{SH^+} is the thermodynamic dissociation constant of SH⁺, with infinite dilution in water the reference state.

Equating the right sides of eq 3 and 5, and recognizing that for a weakly basic substrate $[S]_{st}$ is virtually the same as $[S]$, we get

$$k_{\psi} = (k_r^0[H^+]/K_{SH^+})(\gamma_S\gamma_H/\gamma_{SH^+})(\gamma_{SH^+}/\gamma_{\ddagger}) \quad (6)$$

The dependence of k_{ψ} on acid concentration is determined by the acid concentration dependence of two activity coefficient ratios, $\gamma_S\gamma_H/\gamma_{SH^+}$ pertaining to equilibrium step 1 and $\gamma_{SH^+}/\gamma_{\ddagger}$ pertaining to reaction step 2.

Thus, the overall medium dependence of rate for a weakly basic substrate is composite, being determined in part by one activity coefficient ratio which, because it concerns an equilibrium, *cannot* be related to reaction mechanism and in part by another ($\gamma_{SH^+}/\gamma_{\ddagger}$) which may be related to mechanism. There is abundant evidence that the dependence of both ratios is strongly dependent on the identity of the substrate and/or the character of the reaction which occurs in step 2. Failure fully to appreciate the composite character of the medium dependence of rate, for weakly basic substrates, was a flaw in early hypotheses seeking to relate medium dependence to reaction mechanism.^{4,5}

For the purpose of getting valid information as to what part of the total medium dependence of rate is attributable to reaction step 2, two approaches may be used. One is to study independently the medium dependence of equilibrium protonation of the weakly basic substrate under kinetic study, or of another substance of the same functional type whose protonation is likely to be governed by virtually the same activity coefficients, and thus to evaluate independently the variation of $\gamma_S\gamma_H/\gamma_{SH^+}$ in eq 6. This approach has been utilized in particular by Yates⁶ and by Scorrano.⁷

The second approach is to study kinetically reactions of strongly basic substrates which are essentially fully protonated at the lowest acid concentration of interest.

(5) J. F. Bunnett, *J. Amer. Chem. Soc.*, **83**, 4968 (1961).

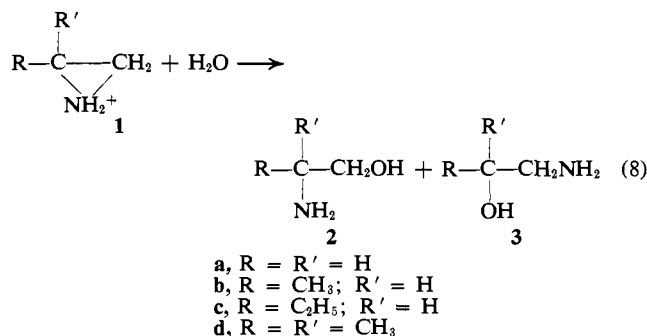
(6) K. Yates, *Accounts Chem. Res.*, **4**, 136 (1971).

(7) G. Scorrano, *Accounts Chem. Res.*, **6**, 132 (1973).

In this case $[S]_{st}$ is virtually equal to $[SH^+]$, and from eq 3 and 4 one obtains

$$k_{\psi} = k_r^0 \gamma_{SH^+} / \gamma_{\pm} \quad (7)$$

It is the second approach that is applied in the present work, with attention to the hydrolytic ring opening of aziridine (**1a**) and its 2-methyl (**1b**) and 2,2-dimethyl (**1d**) derivatives.



The acid-catalyzed hydrolysis of aziridine and its 2-alkyl and 2,2-dialkyl derivatives was earlier studied by Buist and Lucas⁸ and by Earley, *et al.*⁹ On the basis of good evidence, they agreed that the aziridinium ions (**1**), not the aziridines, suffer the actual hydrolysis, that water opens the ring of **1a** by SN2 displacement on carbon, and that the greater part of the hydrolysis of 2,2-dimethylaziridinium ion (**1d**) occurs *via* SN1 heterolysis of the bond between nitrogen and the tertiary carbon atom.¹⁰ However, about 19% of the hydrolysis product from **1d** was reported⁹ to be 2-amino-2-methyl-1-propanol (**2d**), unlikely to result from an SN1 reaction.

The two groups of workers were less emphatic in their views regarding hydrolysis of 2-alkylaziridinium ions. They assigned the SN2 mechanism to scission at primary carbon, but considered the reaction at secondary carbon to be partially if not totally SN1.

The present investigation comprises both kinetic and product studies. The rates of hydrolysis of **1a**, **1b**, and **1d** have been measured in aqueous HClO₄ solutions to *ca.* 6 M, and for **1d** also in aqueous H₂SO₄ to 7 M. For **1a**, the temperature dependence of hydrolysis rates has been measured in 1, 4, and 6 M HClO₄. For **1a** and **1d**, the solvent isotope effect on hydrolysis rates has been determined by comparing rates in 1 M D₂SO₄ (in D₂O) with those in 1 M H₂SO₄ (in H₂O). Finally, product compositions (**2 vs. 3**) have been determined for hydrolysis of **1b** in 0.7–6.1 M HClO₄ and for hydrolysis of **1d** in both HClO₄ and H₂SO₄ up to 4 M.

Experimental Section

Materials. Aziridine, obtained from the Borden Chemical Co., was twice distilled prior to use, bp 56° (lit.⁸ 55° (744 mm)). 2-Methylaziridine, obtained from K&K Laboratories, Inc., was twice distilled prior to use, bp 65° (lit.^{9,11} 63–64). 2,2-Dimethylaziridine, prepared from commercial 2-methyl-2-amino-1-propanol according to the directions of Cairns,¹² was dried over sodium and twice distilled prior to use, bp 71° (lit.⁸ 70.3° (741 mm)). 1-Amino-2-propanol (**3b**), commercial, was distilled prior to use, bp 161° (lit.¹³ 160–161°). 2-Amino-1-propanol (**2b**), prepared by Raney

nickel reduction of 2-nitro-1-propanol formed from the condensation of formaldehyde with nitroethane according to the directions of Vanderbilt and Hass,¹⁴ was distilled prior to use, bp 110° (30 mm) (lit.¹⁵ 76–78° (15 mm)).

N-(2,4-Dinitrophenyl)-1-amino-2-propanol. 1-Amino-2-propanol (100 mg) was added to 5 ml of methanol containing 250 mg of 2,4-dinitrofluorobenzene. After 1 hr at room temperature, the methanol solution was added to 50 ml of water and the product (290 mg; 90%) was collected by filtration. After repeated crystallization from ethanol-water, the melting point was constant at 97°.

Anal. Calcd for C₉H₁₁N₃O₅: C, 44.81; H, 4.56. Found:¹⁶ C, 44.65; H, 4.51.

N-(2,4-Dinitrophenyl)-2-amino-1-propanol prepared in the same manner appeared as an oil rather than a solid. This oil was taken up in chloroform and purified by chromatography on alumina. Attempted crystallization from a variety of solvents gave oils which solidified on long standing. The melting point, 88–93° (lit.¹⁷ 96°), could neither be raised nor sharpened.

Kinetic Procedures. Hydrolysis rate determinations on **1a** and **1b** and some of those on **1d** were made by measuring the disappearance of aziridine with time by the thiosulfate titration method of Earley, *et al.*⁹ At measured times, 5-ml aliquots of the reaction solution (100 ml of standardized 1–6 M perchloric acid containing 1.0–1.5 ml of the aziridine) were withdrawn by pipet and discharged into 100-ml volumetric flasks containing 25 ml of standard 0.05 N aqueous sodium thiosulfate and 35 mequiv of potassium acetate. A precipitate of KClO₄ appeared. The flasks were diluted to the mark and allowed to stand at 30° in a constant-temperature bath for 23 hr. They were then titrated with standard iodine solution (0.05 N) to the iodine or starch end point. The procedure was shown to give an accurate assay for aziridine content for each of the compounds studied by application to solutions of concentration known by previous standardization against standard hydrochloric acid solution. Clean pseudo-first-order kinetics were observed throughout. Rate constants from rate determinations on **1a** in aqueous HClO₄ are presented in Table I, and on **1b** in Table II.

Table I. Rates of Hydrolysis of Aziridine in Perchloric Acid Solutions

Temp, °C	[HClO ₄], ^a M	$k_{\psi} \times 10^7$, sec ⁻¹ b
29.5	0.96	12.85
29.5	0.97	12.78
29.5	1.96	10.85
29.5	1.97	10.85
29.5	2.97	8.87, 8.96, 9.07 ^c
29.5	3.00	8.56
29.5	3.97	6.69, 6.90
29.5	4.02	6.34
29.5	4.98	4.82, 5.04
29.5	5.04	4.60
29.5	5.50	3.73, 4.34
29.5	5.98	3.36, 4.26
29.5	6.05	2.76
49.4	0.96	162.2
49.4	3.97	90.1
49.4	5.98	44.6
67.8	0.96	1311
67.8	3.97	709
67.8	5.98	365

^a HClO₄ concentrations are corrected for the amount used in protonation of aziridine. ^b Duplicate entries represent duplicate runs. ^c Run by periodate titration method.

The periodate titration method of Buist and Lucas⁸ was used to follow one **1a** hydrolysis run; the rate constant obtained did not differ significantly from two others under the same conditions by the thiosulfate titration method. It is noteworthy that the one

(8) G. J. Buist and H. J. Lucas, *J. Amer. Chem. Soc.*, **79**, 6157 (1957).
 (9) J. E. Earley, C. E. O'Rourke, L. B. Clapp, J. O. Edwards, and B. C. Lawes, *J. Amer. Chem. Soc.*, **80**, 3458 (1958).
 (10) C. F. D. S. Tarbell and P. Noble, Jr., *J. Amer. Chem. Soc.*, **72**, 2657 (1950).
 (11) G. D. Jones, *J. Org. Chem.*, **9**, 484 (1944).
 (12) T. L. Cairns, *J. Amer. Chem. Soc.*, **63**, 871 (1941).
 (13) L. Henry, *Ber.*, **33**, 3169 (1900).

(14) B. M. Vanderbilt and H. B. Hass, *Ind. Eng. Chem.*, **32**, 34 (1940).
 (15) J. Attenburrow, J. Elks, B. A. Hems, and K. N. Speyer, *J. Chem. Soc.*, 510 (1949).
 (16) Analysis by Micro-Tech Laboratories, Skokie, Ill.
 (17) M. Jutisz, M. Privat de Garilhe, H. Suquet, and C. Fromageot, *Bull. Soc. Chim. Biol.*, **36**, 117 (1954).

Table II. Rates and Products of Hydrolysis of 2-Methylaziridine in Perchloric Acid Solutions at 29.5°

[HClO ₄], ^a <i>M</i>	<i>k</i> _ψ × 10 ⁷ , sec ⁻¹	Products, % ^b	
		2b	3b
0.70	13.2	62	38
0.98	12.4	66	34
1.46	11.8		
1.56		66	34
2.01	10.1	58	42
3.04	7.98	57	43
4.07	6.07	47	53
5.08		43	57
5.10	4.28		
5.57	3.54	49	51
6.12	3.09	48	52

^a HClO₄ concentrations are corrected for the amount used in protonation of 2-methylaziridine. ^b Percentages of total amino alcohols formed are listed.

method determines unreacted aziridine, the other amino alcohol product.

Most of the rate determinations on **1d** hydrolysis were performed with analysis by proton magnetic resonance, using a 60 MHz Jeolco Minimar spectrometer. Reaction solutions were prepared by placing in a volumetric flask (10 or 25 ml) measured volumes of 6.90 *M* HClO₄ or 7.38 *M* H₂SO₄ (standardized by titration), adding distilled water to fill the flasks about ²/₃ full, weighing, cooling with ice, adding 2,2-dimethylaziridine rapidly with shaking, reweighing to determine the amount of the aziridine added, adding distilled water to the mark, and shaking thoroughly. Small samples (*ca.* 1 ml) were withdrawn at measured times and examined in the nmr spectrometer. When partial hydrolysis had occurred, the nmr spectra of the reaction solutions showed two methyl resonances: a singlet for unreacted **1d**, and another singlet *ca.* 12 Hz upfield due to the conjugate acids of **2d** and **3d**. The latter were not resolved in these strongly acidic solutions. Photocopies of the nmr spectra were made on uniform paper and the relative areas of the two methyl peaks were determined by the cut-and-weigh technique. Plots of ln [(wt of **1d** peak plus wt of products peak)/(wt of **1d** peak)] *vs.* time were linear, and their slopes were taken as *k*_ψ.

Rate constants for **1d** hydrolysis, by both the nmr and thiosulfate titration techniques, are listed in Table III.

Solvent Isotope Effect. Deuteriosulfuric acid, 2 *M*, was prepared by distilling sulfur trioxide (Baker and Adamson Sulfan B) into >99.7% deuterium oxide. This acid was standardized and an amount was added to a 10-ml volumetric flask such that, after dilution to the mark, [D₂SO₄] would be 1 *M*. Aziridine or 2,2-dimethylaziridine (0.2 ml) was added, and the flask was diluted to the mark with D₂O and it was placed in the thermostat; the thiosulfate titration technique was used as described above, except that 1-ml aliquots were taken and the potassium acetate, Na₂S₂O₃, and I₂ were all diluted fivefold. A similar reaction solution in ordinary H₂SO₄ was treated in an identical manner. Data are presented in Table IV.

Analysis of Products from 2-Methylaziridine. Preliminary investigations showed the following. 1-Amino-2-propanol (**3b**) reacted nearly quantitatively with 2,4-dinitrofluorobenzene in aqueous methanol while 2-amino-1-propanol (**2b**) with the same reagent gave lower and variable yields. The *N*-dinitrophenyl derivatives of these amino alcohols could be separated well from impurities by chromatography on alumina but could not be well separated from one another. Once pure, each compound could be recovered quantitatively from alumina. The dinitrophenyl derivative of 2-amino-1-propanol had a modest band in the infrared at 11.55 μ which was absent in the derivative of 1-amino-2-propanol. (A methylene chloride solution containing about 3% of the compound was examined in 1-mm matched cells) Less definite differences also appeared at 9.98 and 10.45 μ. Both amino alcohols could be accurately determined by the periodate titration of Buist and Lucas.⁸ The rates of reaction of the two with periodate were about the same.

With attention to the above findings, an analytical scheme was devised and used to establish product ratios at various HClO₄ concentrations. The total amino alcohol concentration for each sample (2-methylaziridine in perchloric acid after 8 months at reaction temperature) was determined by titrating an aliquot with sodium periodate as described by Buist and Lucas, the periodate solution having been standardized against a 1:1 mixture of **2b** and **3b**. The

Table III. Rates and Products of Hydrolysis of 2,2-Dimethylaziridine in Perchloric and Sulfuric Acid Solutions at 29.5°

Acid (HX)	[HX], ^a <i>M</i>	Method ^b	<i>k</i> _ψ × 10 ⁷ , sec ⁻¹	Products, %	
				2d	3d
HClO ₄	0.52	Nmr	68.4	13.5	86.5
	0.96	Nmr	73.3	10.3	89.7
	0.96	Tit.	68.6		
	1.53	Nmr	63.9	9.9	90.1
	1.96	Tit.	67.3		
	2.05	Nmr	69.6	7.3	92.7
	2.49	Nmr	63.5	6.5	93.5
	2.87	Nmr	66.0	5.4	94.6
	2.97	Tit.	65.9		
	3.97	Tit.	69.1		
	3.98	Nmr	74.8	<4	>96
	4.98	Tit.	82.8		
	5.05	Nmr	90.3	<i>c</i>	<i>d</i>
	5.98	Tit.	127.5		
	6.04	Nmr	151	<i>c</i>	<i>d</i>
	6.54 ^e	Nmr	162	<i>c</i>	<i>d</i>
H ₂ SO ₄	1.05	Nmr	75.1	11.4	88.6
	1.48	Nmr	76.0	8.4	91.6
	1.78	Nmr	77.2	8.9	91.1
	2.50	Nmr	74.4	7.5	92.5
	2.98	Nmr	77.7	5.1	94.9
	3.96	Nmr	71.9	5.4	94.6
	5.02	Nmr	76.8	<i>c</i>	<i>d</i>
	6.96 ^e	Nmr	88.5	<i>c</i>	<i>d</i>

^a HClO₄ and H₂SO₄ concentrations corrected for the amount used in protonation of 2,2-dimethylaziridine. ^b Thiosulfate titration or nmr; see Experimental Section. ^c Too little to determine. ^d Nearly 100%. ^e On assumption of no volume change on mixing of 6.90 *M* HClO₄ or 7.38 *M* H₂SO₄ with 2,2-dimethylaziridine.

Table IV. Rates of Hydrolysis of Aziridine and 2,2-Dimethylaziridine in H₂SO₄ and D₂SO₄ at 29.5°

Solvent ^a	<i>k</i> _ψ × 10 ⁷ , sec ⁻¹
Aziridine	
0.95 <i>M</i> D ₂ SO ₄ in D ₂ O	10.90
0.95 <i>M</i> H ₂ SO ₄ in H ₂ O	14.97
2,2-Dimethylaziridine	
0.95 <i>M</i> D ₂ SO ₄ in D ₂ O	63.0
0.95 <i>M</i> H ₂ SO ₄ in H ₂ O	77.7

^a Acid concentrations corrected for the amounts used in protonation of aziridine or 2,2-dimethylaziridine.

concentration of **3b** was determined for each sample by isolation and infrared analysis of the products of reaction of an aliquot with dinitrofluorobenzene, as follows. A 10-ml aliquot was discharged into a separatory funnel and titrated with 50% aqueous sodium hydroxide to the pink phenolphthalein end point. The color was discharged by addition of 0.5 g of NaHCO₃ and 10 ml of methanol containing 500 mg of 2,4-dinitrofluorobenzene was added. After 2 days at room temperature, 20 ml of water was added and the solutions were extracted five times with 5-ml portions of chloroform. The combined extracts were placed on 20 ml of alumina and eluted with 85 ml of chloroform to remove contaminants. The mixed *N*-dinitrophenyl derivatives were then obtained free of other materials by eluting with 35 ml of a 3:1 chloroform-methanol solution. The solvent was removed under vacuum, the residue was weighed, and sufficient methylene chloride was added to give a 3% solution. The amount of *N*-(2,4-dinitrophenyl)-1-amino-2-propanol isolated was determined by infrared analysis at 11.55 μ. The amount of **3b** in the original solution was calculated assuming 90% isolation and detection, since pure samples behaved thus. The amount of **2b** was calculated as the difference between the total amino alcohol and the **3b** contents. Application of the technique to mixtures of known composition under similar conditions gave results accurate to about ±5%.

The percentages of **2b** and **3b** formed at several HClO₄ concentrations are given in Table II.

Analysis of Products from 2,2-Dimethylaziridine. After reactions had reached at least 90% completion, aliquots were removed,

chilled with ice, and basified by addition of concentrated aqueous NaOH until the pH exceeded 14. Under these conditions, the methyl protons of **2d** absorb *ca.* 8 Hz upfield from those of **3d**. This was verified by addition of authentic **2d** to one sample. The relative amounts of **2d** and **3d** were determined from the areas under these two nmr peaks by the cut-and-weigh technique described above.

For runs at the lowest and highest concentrations of both HClO₄ and H₂SO₄, investigated, material balance was verified by use of an integration standard. For 0.52 M HClO₄, the standard was aniline present in the reaction mixture from the start of the reaction. For the others, it was an external standard, a capillary tube containing methanol, water, and a few drops of H₂SO₄. The capillary tube was inserted into the nmr tube containing the reaction mixture, and the spectra of both solutions were obtained together in a single scan. The peak area ratios, (imine + products)/standard, were independent of time in all cases.

The percentages of **2d** and **3d** formed at several concentrations of HClO₄ and H₂SO₄ are given in Table III.

Temperatures. Thermostat temperatures were verified with reference to thermometers calibrated by the National Bureau of Standards.

Data Correlations. For plots of $\log k_{\psi}$ vs. ($H_0 + \log [H^+]$), H_0 values of Yates and Wai¹⁸ were used for HClO₄ and of Johnson, Katritzky, and Shapiro¹⁹ at 25° for H₂SO₄, and $[H^+]$ was taken to equal the molar concentration of mineral acid.²⁰ For plots of $\log k_{\psi}$ vs. $\log a_w$, values of $\log a_w$ interpolated from those listed by Bunnett²¹ were employed.

Results

The kinetic data in Table I show that the rate of hydrolysis of the aziridinium ion (**1a**) diminishes steadily as the HClO₄ concentration increases from 1 to 6 M. The isotope effect data in Table IV demonstrate that hydrolysis is somewhat slower in deuterated aqueous acids than in systems of normal isotopic composition.

At three acid concentrations, the hydrolysis rate was determined at three temperatures, as reported in Table I. Activation parameters, reckoned from the measured k_{ψ} values,²² are presented in Table V. They show very

Table V. Activation Parameters for **1a** Hydrolysis

[HClO ₄], M	ΔH^{\ddagger} , kcal/mol	ΔS^{\ddagger} , eu
1.0	24.1	-5.8
4.0	24.2	-6.9
6.0	24.4	-7.5

little change of either ΔH^{\ddagger} or ΔS^{\ddagger} with HClO₄ concentration.

The overall rate of hydrolysis of the 2-methylaziridinium ion (**1b**) closely resembles that of **1a**. Data in Tables I and II show that both the absolute rate constants and the pattern of variation with HClO₄ concentration are nearly the same for the two substrates. There is some change in the relative amounts of **2b** and **3b** produced, in the sense that the fraction of **3b** increases with acid concentration, but the change is modest.

In HClO₄ solutions, the overall rate of hydrolysis of the 2,2-dimethylaziridinium ion (**1d**) is considerably greater than of **1a** or **1b**; see Table III. It remains

(18) K. Yates and H. Wai, *J. Amer. Chem. Soc.*, **86**, 5408 (1964).

(19) C. D. Johnson, A. R. Katritzky, and S. A. Shapiro, *J. Amer. Chem. Soc.*, **91**, 6654 (1969).

(20) J. F. Bunnett and F. P. Olsen, *Can. J. Chem.*, **44**, 1899 (1966).

(21) J. F. Bunnett, *J. Amer. Chem. Soc.*, **83**, 4956 (1961).

(22) J. F. Bunnett in "Investigation of Reaction Rates and Mechanisms," 2nd ed, Part I, S. L. Friess, E. S. Lewis, and A. Weissberger, Ed., Interscience, New York, N. Y., 1961, p 201.

nearly constant between 0.5 and 4 M HClO₄, but then rises rather sharply with further increase in acid concentration. The pattern in H₂SO₄ is similar, except that the initial plateau extends to 5 M H₂SO₄ and the final rise is less steep. In both systems, the hydrolysis product is about 12% **2d** in rather dilute acid, and the fraction of this product diminishes steadily so that it can scarcely be detected at acid concentrations above 4 M.

Comparison with Other Measurements. From the data of Earley, *et al.*,⁹ for aziridine hydrolysis in *ca.* 0.7 M HClO₄, we interpolate $11.8 \times 10^{-7} \text{ sec}^{-1}$ as the rate constant at 29.5°. Extrapolation of our data at 29.5° to 0.7 M gives $13.0 \times 10^{-7} \text{ sec}^{-1}$. For hydrolysis of 2,2-dimethylaziridine in 0.7 M HClO₄ at 29.5°, $7.3 \times 10^{-6} \text{ sec}^{-1}$ is interpolated from their data and $7.0 \times 10^{-6} \text{ sec}^{-1}$ from ours. In both cases the agreement is fairly good.

Buist and Lucas⁸ reported hydrolysis of **1b** in 0.04 M HClO₄ at 65° to be *ca.* 10% faster than of **1a**. We find **1a** to hydrolyze about 3% faster than **1b** in 1.0 M HClO₄ at 29.5°. The slight disagreement is no cause for concern.

The products of **1c** hydrolysis in dilute HClO₄ were estimated⁹ to be about 75% 2-amino-1-butanol (**2c**) and 25% 1-amino-2-butanol (**3c**). Our finding that **1b** affords, in 0.7 M HClO₄, 62% of **2b** and 38% of **3b** is in reasonable agreement with that estimate; the structural relationship of **1b** to **1c** is obviously close.

Earley, *et al.*,⁹ used two methods to estimate the percentages of **2d** and **3d** formed on hydrolysis of **1d** in dilute HClO₄ solutions. By fractional distillation and refractive index measurement, they estimated the product mixture to comprise 15% of **2d** and 85% of **3d**. From potentiometric titration, they estimated 23% of **2d** and 77% of **3d**. Our determination by nmr that 13.5% of **2d** and 86.5% of **3d** are formed in 0.52 M HClO₄ is quite close to theirs by the fractional distillation method of analysis.

Discussion

Methods for Correlation of Data. It would be unrewarding to plot $\log k_{\psi}$ for a strongly basic substrate against H_0 or other acidity function, as is sometimes done for reactions of weakly basic substrates. The rationale for such plots is that the extent of protonation of a weakly basic substrate is in some fashion related to H_0 , but **1a**, **1b**, and **1d** are already fully protonated in 0.5 M mineral acid.

For many reactions of strongly basic substrates, plots of $\log k_{\psi}$ against ($H_0 + \log [H^+]$), where H_0 is the Hammett acidity function,^{4b, 18, 19} are linear.²³ Equation 9 is obeyed. The slope constitutes a parameter, ϕ ,

$$\log k_{\psi} = \phi(H_0 + \log [H^+]) + \text{constant} \quad (9)$$

which characterizes the kinetic response of the reaction to changing acid concentration.

It follows from the definition of the Hammett acidity function,^{4b} $H_0 \equiv -\log (a_H + \gamma_B/\gamma_{BH^+})$, that ($H_0 + \log [H^+]$) equals $\log (\gamma_{BH^+}/\gamma_B\gamma_{H^+})$. Comparison with the logarithmic form of eq 7 shows that ϕ , the proportionality constant in eq 9, is therefore also a proportionality constant between the logarithms of activity coefficient ratios as they vary with mineral acid concentration.²³

(23) J. F. Bunnett and F. P. Olsen, *Can. J. Chem.*, **44**, 1917 (1966).

Table VI. Rate Correlations

Reaction	Acid	Temp, °C	Horizontal coordinate	Slope ^a (ϕ or w)	Intercept	Statistical parameters ^b		
						σ_y	σ_{s1}	r
1a → 2a	HClO ₄	29.5	($H_0 + \log [H^+]$)	0.33	-5.78	0.035	0.014	0.986
			Log a_w	1.81		0.044	0.09	0.978
		49.4	($H_0 + \log [H^+]$)	0.31	-4.69	0.007	0.005	0.9998
			Log a_w	1.76		0.041	0.18	0.995
		67.8	($H_0 + \log [H^+]$)	0.31	-3.78	0.001	0.001	0.9999
			Log a_w	1.76		0.049	0.22	0.992
1b → 2b	HClO ₄	29.5	($H_0 + \log [H^+]$)	0.42	-5.98	0.048	0.024	0.989
			Log a_w	2.39		0.078	0.22	0.971
1b → 3b	HClO ₄	29.5	($H_0 + \log [H^+]$)	0.23	-6.27	0.039	0.019	0.977
1d → 2d	HClO ₄	29.5	($H_0 + \log [H^+]$)	0.69	-5.90	0.024	0.045	0.987
			Log a_w	5.92		0.022	0.35	0.990
1d → 3d	HClO ₄	29.5	($H_0 + \log [H^+]$)	-0.20	-5.21 ^c	0.057	0.021	0.930
			Log a_w	-1.11		0.041	0.08	0.964
1d → 2d	H ₂ SO ₄	29.5	($H_0 + \log [H^+]$)	0.38	-5.99	0.051	0.067	0.942
			Log a_w	2.75		0.063	0.63	0.909
1d → 3d	H ₂ SO ₄	29.5	($H_0 + \log [H^+]$)	-0.05	-5.17 ^d	0.023	0.012	0.860
			Log a_w	-0.26		0.019	0.05	0.900

^a Slope is ϕ vs. ($H_0 + \log [H^+]$), or w vs. $\log a_w$. ^b σ_y is standard deviation of points, in the y direction, from the least-squares line; σ_{s1} is standard deviation of the slope; r is correlation coefficient. ^c From points through 2.97 M HClO₄ only. ^d From points through 5.02 M H₂SO₄ only.

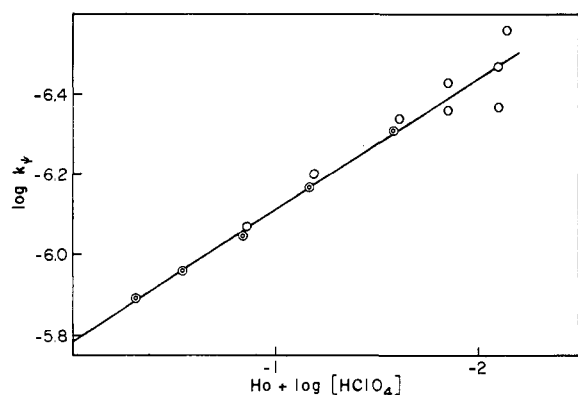


Figure 1. Plot of $\log k_\psi$ for 1a hydrolysis in HClO₄ against ($H_0 + \log [H^+]$). Bulls eyes represent duplicate determinations. The linear regression line is drawn.

The medium dependence of reaction rates can alternatively be expressed by the w parameter, which for strongly basic substrates is the slope of the linear or approximately linear plot of $\log k_\psi$ vs. $\log a_w$, where a_w is the activity of water.²¹ If appropriate assumptions are made about the medium dependence of the activity coefficients for hydrated SH⁺ and transition state,²⁴ the w value may be taken as an indication of the average number of water molecules difference of hydration between the two states.²⁵

Rate Correlations. For all the sets of data in Tables I–III, we have correlated $\log k_\psi$ both with ($H_0 + \log [H^+]$) and with $\log a_w$. The results of linear regression analysis are summarized in Table VI. Three selected correlations are also plotted, in Figures 1–3.

The overall k_ψ values for 1b and 1d hydrolysis were dissected into components representing formation of each of the isomeric amino alcohol products, in proportion to the yields of those products. The dissected rather than the overall rate constants are correlated in those cases.

Most of the correlations are good rather than superb,

(24) The activity coefficients for hydrated species are different from those for formal species, which are the type usually employed.²⁵

(25) J. F. Bunnett, *J. Amer. Chem. Soc.*, **83**, 4973 (1961).

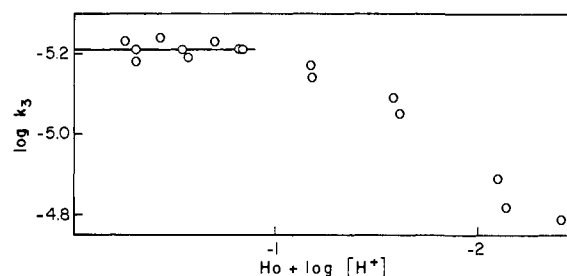


Figure 2. Plot of $\log k_\psi$ for the 1d → 3d reaction in HClO₄ vs. ($H_0 + \log [H^+]$). The linear regression line through the left nine points is drawn.

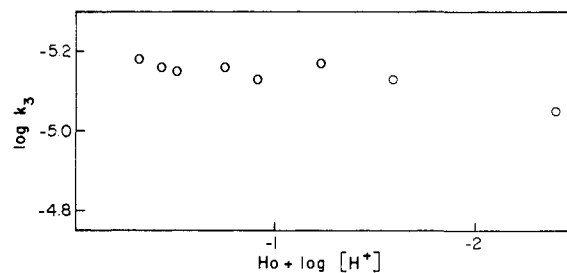


Figure 3. Plot of $\log k_\psi$ for the 1d → 3d reaction in H₂SO₄ vs. ($H_0 + \log [H^+]$).

because of scatter of experimental points. Scatter is evident in Figure 1, in which $\log k_\psi$ for hydrolysis of 1a in HClO₄ solutions at 29.5° is plotted against ($H_0 + \log [H^+]$). The rate constants for formation of 2b and 3b from 1b, and of 2d and 3d from 1d, depend not only on overall k_ψ values but also on the product analysis at each acid concentration, which is a further source of experimental variability. However, the only plot against ($H_0 + \log [H^+]$) which shows any regular curvature is that for hydrolysis of 1d to 3d in HClO₄ solutions (Figure 2).

Inasmuch as the vertical coordinate is the same in plots against ($H_0 + \log [H^+]$) as against $\log a_w$, the comparative quality of fit by the two methods of correlation is best judged by comparison of σ_y parameters,

which are tabulated in Table VI. These show that for most reactions, a better correlation is obtained with $(H_0 + \log [H^+])$ than with $\log a_w$, in agreement with earlier observations. Some of the plots against $\log a_w$ show obvious curvature whereas their counterparts against $(H_0 + \log [H^+])$ are straight.

Let us now consider the constant in eq 9. As the acid becomes more and more dilute, H_0 approaches $-\log [H^+]$ and at infinite dilution they are equal.^{4b} Therefore the constant is $\log k_r^0$; see eq 7. Substituting into eq 9

$$\log k_\psi = \phi(H_0 + \log [H^+]) + \log k_r^0 \quad (10)$$

The intercepts in such plots, which are listed in Table VI, are therefore $\log k_r^0$, the rate constants for hydrolysis of the relevant *aziridinium ions* at infinite dilution in water. Because plots against $\log a_w$ are less straight, they are less satisfactory for extrapolation to infinite dilution and the intercepts therefore are not listed.

For the two plots in Figures 2 and 3, intercepts were reckoned by linear regression analysis applied only to points in the initial flat portions of the plots. The statistical parameters for analysis of the short set of data for 0.52–2.97 *M* HClO₄ are instructive. The correlation coefficient (*r*) is 0.023, suggesting a horrible correlation, but the σ_y of 0.021 shows that the quality of fit to a straight line is much better than when linear regression analysis is applied to data covering the whole range of 0.52–6.54 *M*, for which σ_y is 0.057. However, *r* for the latter is 0.930, as listed in Table VI. The explanation lies in the fact that the slope (ϕ) for the short set is only 0.002. The correlation coefficient was developed by social scientists as an index of whether two variables are correlated, and the social scientist would conclude in the case of the short set that there is no correlation. The natural scientist, in contrast, sees it as a fair correlation with essentially zero slope. The natural scientist is thus better informed, in comparing two methods of correlation involving the same vertical coordinate, by σ_y than by *r*.

The intercepts in Table VI for the **1d** → **2d** reaction in HClO₄ and H₂SO₄ should be the same, namely, k_r^0 (see eq 10). Likewise, the intercepts for the **1d** → **3d** reaction should be identical. Statistical analysis reveals, for each comparison, that the actual discrepancy only slightly exceeds the sum of the standard deviations of the two intercepts. The discrepancies are thus within experimental error.

Interpretation of Correlations. Our interest is to assess the extent to which medium dependence of rate, that is, of the activity coefficient ratio in eq 7, is related to reaction mechanism and what part stems from other factors. For this purpose, we shall consider the experimentally determined medium dependence, as represented by the ϕ parameter, with respect to the prevailing reaction mechanism as indicated by independent criteria.

Following earlier workers,^{8,9} as discussed above, we acknowledge hydrolytic cleavage of the C–N bond to occur by the SN2 mechanism at primary carbon (in **1a** and at the terminal carbon atoms of **1b** and **1d**) and by the SN1 mechanism at the tertiary carbon atom of **1d**. Though we do not wish to concern ourselves with the finer details of these mechanisms, we do note that once the bond in **1d** between nitrogen and tertiary carbon

has parted it is unlikely to re-form rapidly in comparison with events that consummate hydrolysis. Ring strain would cause the carbon and nitrogen atoms to spring apart once the bond had broken, and the nature of the medium is such as to ensure rapid protonation of the amino group of the resulting carbonium ion.

As for the mechanism of scission of the bond between nitrogen and secondary carbon in **1b**, we shall for the moment take no position. The mechanism of nucleophilic substitution at secondary aliphatic carbon is controversial.

If there were a simple, direct relationship of ϕ value to mechanism, the ϕ values for the SN2 processes (**1a** → **2a**, **1b** → **2b**, and **1d** → **2d**) would be equal, except as affected by experimental error. However, they are not equal; in HClO₄ at 29.5°, they are +0.33, +0.42, and +0.69, respectively. This is a wide spread. We must conclude either that the ϕ value has no close intrinsic relationship to reaction mechanism or that in the present case effects of other origin also substantially affect the activity coefficient ratio in eq 7.

It is noteworthy that the ϕ value for conversion of **1d** to **2d** in H₂SO₄ (+0.38) lies between those for the **1a** → **2a** and **1b** → **2b** reactions in HClO₄. These three ϕ values, for hydrolyses by the SN2 mechanism, fall within a relatively narrow spread of 0.09. Attention should therefore perhaps be focused on the difference in ϕ values for the **1d** → **2d** transformation between HClO₄ and H₂SO₄.

The plot of $\log k_\psi$ vs. $(H_0 + \log [H^+])$ for hydrolytic scission of **1d** at tertiary carbon in HClO₄ (Figure 2) is markedly curved; the slope is zero at low acid concentrations and about –0.36 above 4 *M* HClO₄. Curvature in such plots can arise from a change in reaction mechanism,^{6,23} but in the present case it is difficult to conceive of a further mechanism that could supersede SN1 at the higher HClO₄ concentrations. Also, if there were a change of mechanism, similar curvature should appear in the corresponding plot for H₂SO₄, but that plot (Figure 3) is almost straight. We seem forced to conclude that the curvature in Figure 2 stems from activity coefficient effects not related to reaction mechanism.

We may then inquire whether the exceptionally high ϕ value for the **1d** → **2d** conversion in HClO₄ solutions also represents an activity coefficient effect unrelated to mechanism.

Differences between HClO₄ and H₂SO₄, as they affect kinetic response to changing acid concentration, have been noted many times before. For some reactions, the kinetic response (as judged by the ϕ value or other appropriate parameter) is nearly the same in the two acids,²⁶ but in others it is remarkably different.²⁷ Moreover, although plots of $\log k_\psi + H_0$ (for weakly basic substrates) or $\log k_\psi$ (for strongly basic substrates) vs. $(H_0 + \log [H^+])$ are usually straight, instances of curvature for HClO₄ have been encoun-

(26) C. A. Bunton, S. J. Farber, A. J. G. Milbank, C. J. O'Connor, and T. A. Turney, *J. Chem. Soc., Perkin Trans. 2*, 1869 (1972); D. Landini, G. Modena, U. Quintily, and G. Scorrano, *J. Chem. Soc. B*, 2041 (1971); J. W. Barnett and C. J. O'Connor, *J. Chem. Soc., Perkin Trans. 2*, 220 (1973); C. J. Hyland and C. J. O'Connor, *ibid.*, 233 (1973).

(27) (a) C. A. Bunton, J. H. Crabtree, and L. Robinson, *J. Amer. Chem. Soc.*, **90**, 1258 (1968); (b) C. A. Bunton and E. Humeres, *J. Org. Chem.*, **34**, 572 (1969); (c) A. J. Kresge, S. G. Mylonakis, and L. E. Hakka, *J. Amer. Chem. Soc.*, **94**, 4197 (1972).

tered.^{28,29} There are also some irregularities in LFER correlation of equilibrium protonation in HClO_4 , in contrast to the prevailing regular behavior in H_2SO_4 .²⁰

Bunton, Crabtree, and Robinson^{27a} pointed out that A-1 reactions tend to go faster in HClO_4 than in H_2SO_4 but that A-2 reactions tend to be faster in H_2SO_4 . They attributed this behavior in part to a propensity of perchlorate ion, a large ion of low charge density, to associate preferentially with carbonium ions, actual or partially formed in a transition state. They also consider that transition states with little or no carbonium ion character but with good sites for (donor) hydrogen bonding with the medium will be favored in mineral acids having anions of higher charge density (e.g., HSO_4^- or Cl^-).

Kresge, *et al.*,^{27c} on the other hand, think that hydrogen isotope exchange in 1,3-dimethoxybenzene is faster in H_2SO_4 than in HClO_4 because there is a component of general acid catalysis by bisulfate ion; perchlorate ion could not be a general acid. However, they did not extend their hypothesis to reactions of other classes of substrates.

Our data for **1d** hydrolysis (Table III) indicate that formation of **2d** is faster, at higher acid concentrations, in H_2SO_4 than in HClO_4 , and that formation of **3d** is faster in HClO_4 . Qualitatively, these inequalities are in accord with the generalization of Bunton, Crabtree, and Robinson.^{27a}

There is thus reason to suspect that the curvature in Figure 2 and the exceptionally high ϕ value for the **1d** \rightarrow **2d** transformation in HClO_4 are the consequence of unusual activity coefficient effects. If for that reason the ϕ values for **1d** hydrolysis in HClO_4 are disregarded, the remaining ϕ values in Table VI may be taken to indicate that in this system the $\text{S}_{\text{N}}1$ mechanism is associated with a ϕ value of about -0.05 and the $\text{S}_{\text{N}}2$ with a ϕ of about $+0.35$. There is also a suggestion that H_2SO_4 is a better medium than HClO_4 for study of acid concentration effects on rate, if they are to be taken as an indication of mechanism.

(28) C. A. Bunton and J. H. Fendler, *J. Org. Chem.*, **30**, 1365 (1965).

(29) C. A. Bunton and L. Robinson, *J. Amer. Chem. Soc.*, **91**, 6072 (1969).

With these tentative conclusions in mind, let us now look at the **1b** \rightarrow **3b** conversion. The ϕ value (in HClO_4) lies closer to that associated with the $\text{S}_{\text{N}}2$ than with the $\text{S}_{\text{N}}1$ mechanism. This suggests that the mechanism is basically $\text{S}_{\text{N}}2$. If the C-O bond is less formed at the transition state than for reaction at primary carbon, less hydration of the attacking water molecule may be expected, and therefore a lower ϕ value.²⁵ There might also be some steric interference with solvation.

Temperature Effects. For hydrolysis of **1a**, $\log k_{\psi}$ was correlated with $(H_0 + \log [\text{H}^+])$ or $\log a_w$ at 49.4 and at 67.8°, as well as at 29.5°; see Table VI. Data for the horizontal coordinates are all for *ca.* 25°. The correlations at the higher temperatures are somewhat better than at 29.5°, and the slope parameters are nearly the same.

As for the activation parameters (Table V), ΔH^{\ddagger} is nearly the same at 1, 4, and 6 *M* HClO_4 . There is, however, a moderate trend in the apparent entropy of activation. We say "apparent" because the value of ΔS^{\ddagger} depends on the absolute magnitude of the rate constants from which it is calculated.²² Inasmuch as water is a reactant in **1a** hydrolysis and the activity of water decreases as the acid concentration increases, it would be better to calculate ΔS^{\ddagger} from corrected rate constants, k_{ψ}' , where $k_{\psi}' = k_{\psi}/a_w^m$, m being the order of the reaction in water. However, because m is not known with certainty and may change with acid concentration, we do not list corrected ΔS^{\ddagger} values. Some trial computations indicate that the corrected ΔS^{\ddagger} values would show a lesser decrease with augmenting acid concentration, or even a modest increase.

At least part of the negative entropy of activation represents immobilization of water molecules bound into the transition state. The entropy of freezing of water is -5.26 gibbs/mol. Therefore, if the w value of *ca.* 1.8 for **1a** hydrolysis (Table VI) is taken literally as the kinetic order in water, the contribution of water immobilization to entropy of activation may be estimated as $(1.8)(-5.26)$ or -9.5 gibbs/mol. This is somewhat more negative than the measured ΔS^{\ddagger} values.